

Attorney Docket No. 82985  
Customer No. 23523

ITERATIVE DECISION FEEDBACK ADAPTIVE EQUALIZER

TO WHOM IT MAY CONCERN:

BE IT KNOWN THAT (1) FLETCHER A. BLACKMON, employee of the United States Government, citizen of the United States of America, and (2) MOHAMADREZA M. HAGH, (3) JOHN PROAKIS, and (4) MASOUD SALEHI, citizens of the United States, residents of (1) Forestdale, County of Barnstable, Commonwealth of Massachusetts, (2) Belmont, County of Middlesex, Commonwealth of Massachusetts, (3) Andover, County of Essex, Commonwealth of Massachusetts and (4) Westwood, County of Norfolk, Commonwealth of Massachusetts, have invented certain new and useful improvements entitled as set forth above of which the following is a specification:

JAMES M. KASISCHKE, ESQ.  
Reg. No. 36562  
Naval Undersea Warfare Center  
Newport, RI Division Newport 02841-1708  
TEL: 401-832-4736  
FAX: 401-832-1231

I hereby certify that this correspondence is being deposited with the U.S. Postal Service as U.S. EXPRESS MAIL, Mailing Label No. EL578538975US. In envelope addressed to: Commissioner for Patents, Alexandria, VA 22313 on 18 Sept. 2003  
(DATE OF DEPOSIT)

Orin K. Ogden  
APPLICANT'S ATTORNEY

18 Sept. 2003  
DATE OF SIGNATURE

1 Attorney Docket No. 82985

2

3 ITERATIVE DECISION FEEDBACK ADAPTIVE EQUALIZER

4

5 This application claims the benefit of United States  
6 Provisional Application No. 60/412,432, filed 20 September 2002.

7

8 STATEMENT OF GOVERNMENT INTEREST

9 The invention described herein may be manufactured and used  
10 by or for the Government of the United States of America for  
11 governmental purposes without the payment of any royalties  
12 thereon or therefore.

13

14 BACKGROUND OF THE INVENTION

15 (1) Field of the Invention

16 The present invention relates generally to communications  
17 systems and, more particularly, to a high performance iterative  
18 and adaptive decision feedback equalizer which is especially  
19 suitable for use in underwater telemetry.

20 (2) Description of the Prior Art

21 The underwater environment provides numerous difficult  
22 obstacles for acoustic communications. The ocean acoustic  
23 channel produces large amplitude and phase fluctuations on  
24 acoustic signals transmitted therethrough causing temporal,  
25 spatial, and frequency dependent fluctuations. Multipath

1 distortion is a significant problem. Underwater regions often  
2 experience high and/or variable sound attenuation. Ambient ocean  
3 noise influences the received signal-to-noise ratio and may  
4 require high transmission power levels to achieve suitable ratios  
5 depending on the conditions.

6 Presently utilized underwater coherent acoustic telemetry  
7 systems are often able to transmit M-ary Phase Shift Keying  
8 (MPSK) and M-ary Quadrature Amplitude Modulation (MQAM) signals.

9 At the receiver end, these coherent signals may be processed by  
10 an adaptive multi-channel decision feedback equalizer (DFE). The  
11 DFE is then usually followed by a de-interleaver and an error  
12 correction decoder operating in a single pass fashion. The de-  
13 interleaver randomizes the errors and the error correction  
14 decoder tries to correct these randomly distributed errors. The  
15 error correction decoder is usually a Viterbi decoder for a  
16 convolutional code. The overall performance obtained by this  
17 type of prior art underwater telemetry system is often  
18 acceptable, but is not satisfactory in many situations. The  
19 desire for performance improvement has led to higher performance  
20 algorithms whose complexity is orders of magnitude greater than  
21 the standard decision feedback equalizer (DFE) system followed by  
22 de-interleaving and decoding. The turbo-equalization algorithm  
23 is one such algorithm that has performed much better than the  
24 normal algorithm but the cost has been extremely high complexity.

1 Turbo equalization and turbo coding may be applied to many  
2 detection and decoding problems. Turbo coding involves  
3 concatenation of simple component codes with an interleaver so  
4 that decoding can be performed in steps using algorithms of  
5 manageable complexity. However, the complexity of prior art  
6 turbo equalization increases exponentially with the number of  
7 channels and/or other factors, thereby making a multichannel  
8 telemetry system, as is typically utilized in underwater  
9 telemetry systems, highly complex. More particularly, the  
10 complexity of the prior art turbo-equalizer grows with channel  
11 complexity, modulation level, and spatial and/or time diversity.  
12 The complexity of a prior art turbo-equalizer is therefore  
13 orders of magnitude greater than the typical DFE structure  
14 discussed above.

15 The following U.S. Patents describe various prior art  
16 systems that may be related to the above and/or other telemetry  
17 systems:

18 U.S. Patent No. 5,301,167, issued April 5, 1994, to Proakis  
19 et al., discloses an underwater acoustic communications system  
20 that utilizes phase coherent modulation and demodulation in which  
21 high data rates are achieved through the use of rapid Doppler  
22 removal, a specialized sample timing control technique and  
23 decision feedback equalization including feedforward and feedback  
24 equalizers. The combined use of these techniques dramatically  
25 increases data rates by one and sometimes two orders of magnitude

1 over traditional FSK systems by successfully combating fading and  
2 multipath problems associated with a rapidly changing underwater  
3 acoustic channel that produce intersymbol interference and makes  
4 timing optimization for the sampling of incoming data impossible.

5 U.S. Patent No. 5,559,757, issued September 24, 1996, to  
6 Catipovic et al., discloses an underwater acoustic telemetry  
7 system that uses spatially distributed receivers with aperture  
8 sizes from 0.35 to 20 m. Output from each receiver is assigned a  
9 quality measure based on the estimated error rate, and the data,  
10 weighted by the quality measure, is combined and decoded. The  
11 quality measure is derived from a Viterbi error-correction  
12 decoder operating on each receiver. The quality estimator  
13 exploits the signal and noise differential travel times to  
14 individual sensors. The spatial coherence structure of the  
15 shallow-water acoustic channel shows relatively low signal  
16 coherence at separations as short as 0.35 m. Increasing receiver  
17 spacing beyond 5 m offers additional benefits in the presence of  
18 impulsive noise and larger scale inhomogeneities in the acoustic  
19 field. Diversity combining, even with only two receivers, can  
20 lower uncoded error rates by up to several orders of magnitude  
21 while providing immunity to transducer jamming or failure.

22 U.S. Patent No. 6,295,312 B1, issued September 25, 2001, to  
23 Susan M. Jarvis, discloses a method and system for communicating  
24 in a time-varying medium. A transmitter sends transmissions of  
25 the same message data separated in time with respect to one

1 another. A single sensor receives the transmissions. Each  
2 received transmission is buffered until all of the transmissions  
3 that were sent are received. The buffered transmissions are  
4 simultaneously processed via multichannel adaptive equalization  
5 only when all of the transmissions that were sent are received.

6 The above cited prior art does not disclose a system whose  
7 complexity is similar to that of the prior art decision feedback  
8 equalizer followed by a de-interleaver and an error correction  
9 decoder, but whose performance is greatly improved. The above  
10 cited prior art also does not disclose decision feedback  
11 equalizers utilizing hard and/or soft feedback from the decoder.  
12 The solutions to the above described and/or related problems have  
13 been long sought without success. Consequently, those skilled in  
14 the art will appreciate the present invention that addresses the  
15 above and other problems.

16

#### 17 SUMMARY OF THE INVENTION

18 It is a general purpose of the present invention to provide  
19 an improved telemetry system.

20 Yet another object is to provide an augmented high  
21 performance iterative receiver algorithm for underwater acoustic  
22 telemetry.

23 It is another object of the present invention to provide a  
24 hard-iterative DFE structure and a soft-iterative DFE structure  
25 that is superior to the standard DFE structure.

1        It is yet another object of the present invention to provide  
2 a system which has linear complexity growth with the size of the  
3 symboling constellation as opposed to more complex systems such  
4 as turbo-equalization which experience exponential complexity  
5 growth.

6        An advantage of the present invention is that it takes  
7 advantage of the attractive features of the DFE structure such as  
8 diversity combining, modest complexity increase with channel  
9 complexity, symbol synchronization, and phase tracking while  
10 providing higher performance than a standard DFE with less  
11 complexity than the turbo-equalizer.

12       A feature of one embodiment of the invention combines a  
13 decision feedback adaptive equalizer (DFE) with a turbo-equalizer  
14 whereby the decision feedback equalizer or variant thereof  
15 provides a pre-processing stage for a turbo-equalizer that  
16 significantly limits the complexity of the turbo-equalizer.

17       An advantage of the present invention is superior  
18 performance as compared to the standard DFE structure.

19       Another advantage is that time or spatial signal diversity  
20 can be processed with low complexity within the DFE to provide a  
21 single stream of diversity combined symbols which can be  
22 processed with a simplified turbo-equalizer construction for use  
23 in multichannel transmissions.

1        Yet another advantage of the present invention is that a DFE  
2 structure may be utilized therein to take advantage of fractional  
3 spacing to help synchronize symbols.

4        Yet another advantage of the present invention is that a DFE  
5 structure may be utilized to reduce the extent of the channel  
6 response and therefore allow a turbo-equalizer to operate on a  
7 much shorter impulse response in order to reduce the complexity  
8 thereof.

9        These and other objects, features, and advantages of the  
10 present invention will become apparent from the drawings, the  
11 descriptions given herein, and the appended claims. However, it  
12 will be understood that above listed objects and advantages of  
13 the invention are intended only as an aid in understanding  
14 certain aspects of the invention, are not intended to limit the  
15 invention in any way, and do not form a comprehensive or  
16 exclusive list of objects, features, and advantages.  
17 Accordingly, the present receiver is operable for use in a  
18 telemetry system such as an underwater telemetry system and may  
19 comprise one or more elements such as, for instance, at least one  
20 data input channel connected to the receiver, and a decision  
21 feedback equalizer for receiving the data input channel. The  
22 present receiver preferably produces an estimated symbol sequence  
23 output during a plurality of iterations of operation. The  
24 present receiver may further comprise a symbol-by-symbol detector  
25 which is preferably operable for receiving the estimated symbol



1 sequence output and operable to produce a symbol-by-symbol  
2 detector output. A decoder is provided for receiving the  
3 estimated symbol sequence output and for producing a decoded  
4 output. An iterative feedback connection is provided between the  
5 decoder and the decision feedback equalizer to provide feedback  
6 from the decoder for use in at least some of the plurality of  
7 iterations of operation of the decision feedback equalizer. In a  
8 preferred embodiment, the decoder may be a Viterbi decoder or a  
9 MAP decoder.

10 The receiver further may comprise a feedback filter for the  
11 decision feedback equalizer and in one embodiment may comprise a  
12 switch between the symbol-by-symbol detector and the feedback  
13 filter and the iterative feedback connection operable for  
14 selectively connecting the symbol-by-symbol detector output to  
15 the feedback filter or for connecting the iterative feedback  
16 connection to the feedback filter. In this embodiment, the  
17 switch is operable for connecting the symbol-by-symbol detector  
18 output to the feedback filter during a first iteration of the  
19 plurality of iterations and then connecting the iterative  
20 feedback connection to the feedback filter for subsequent of the  
21 plurality of iterations, at least until a stop criterion is  
22 reached.

23 The receiver may further comprise a feedback filter wherein  
24 the feedback filter is operable for receiving hard values of

1 decoded symbols from the decoder by means of the iterative  
2 feedback connection.

3       In another embodiment the iterative feedback connection  
4 between the decoder and the decision feedback equalizer may  
5 connect to the symbol-by-symbol detector. The iterative feedback  
6 connection provides log likelihood ratio information and the  
7 symbol-by-symbol detector may further comprise a converter for  
8 converting estimated symbol sequence output from said decision  
9 feedback equalizer to log likelihood ratio information. A  
10 combiner may be utilized to combine the log likelihood ratio  
11 information from the iterative feedback connection and the log  
12 likelihood ratio information produced by the converter. The  
13 symbol-by-symbol detector further comprises a decision module for  
14 receiving the combiner output and producing hard values of  
15 decoded symbols for the feedback filter.

16       A method of operation is provided which may comprise one or  
17 more steps such as, for instance, iteratively processing a  
18 received signal with a decision feedback equalizer to produce  
19 estimated symbol sequence information and post-processing the  
20 estimated symbol sequence information with a decoder wherein the  
21 decoder may comprise at least a Viterbi decoder or a MAP decoder.  
22 Other steps may comprise providing a feedback connection between  
23 the decoder and the decision feedback equalizer to provide  
24 feedback information from the decoder for use in at least some

1 plurality of iterations of the processing by the decision  
2 feedback equalizer.

3       The method may further comprise selectively utilizing the  
4 feedback information from the decoder so that after a first  
5 iteration of processing by the decision feedback equalizer, then  
6 the feedback information is utilized in subsequent of the  
7 plurality of iterations of the processing, at least until a stop  
8 criterion is reached.

9       In one possible embodiment, the method may comprise  
10 controlling a switch for connecting the feedback connection to  
11 the feedback filter in the decision feedback equalizer.

12       In another possible embodiment, the method may comprise  
13 combining the estimated symbol sequence information with log  
14 likelihood ratio information produced utilizing the decoder.

15       The method may comprise processing the estimated symbol sequence  
16 information prior to the step of combining by converting the  
17 estimated symbol sequence information to log likelihood ratio  
18 information. The step of converting may further comprise  
19 multiplying the estimated symbol sequence by a factor wherein the  
20 factor comprises computing a variance of the estimated symbol  
21 sequence.

22       The method may comprise iteratively processing BPSK  
23 modulated signals or may comprise iteratively processing MPSK and  
24 MQAM modulated signals and/or may be utilized for other types of  
25 modulated signals, as desired.

1 BRIEF DESCRIPTION OF THE DRAWINGS

2 A more complete understanding of the invention and many of  
3 the attendant advantages thereto will be readily appreciated as  
4 the same becomes better understood by reference to the following  
5 detailed description when considered in conjunction with the  
6 accompanying drawing, wherein like reference numerals refer to  
7 like parts and wherein:

8 FIG. 1 is a block diagram schematic of a presently preferred  
9 iterative decision feedback equalizer with hard feedback in  
10 accord with the present invention;

11 FIG. 2 is a block diagram schematic of a presently preferred  
12 iterative decision feedback equalizer with soft feedback in  
13 accord with the present invention;

14 FIG. 3 is a block diagram schematic of a symbol-by-symbol  
15 detector unit for an iterative decision feedback equalizer with  
16 soft feedback in accord with the present invention; and

17 FIG. 4 is a block diagram schematic of an alternative  
18 embodiment symbol-by-symbol detector for an iterative decision  
19 feedback equalizer with soft feedback for MPSK modulation.  
20

21 DESCRIPTION OF THE PREFERRED EMBODIMENT

22 The present invention provides an augmented high performance  
23 iterative receiver algorithm for underwater acoustic telemetry.

24 The present invention provides an improved performance iterative  
25 decision feedback equalizer (DFE) which may utilize either hard

1 feedback or soft feedback while maintaining reasonable modest  
2 complexity. The complexity of the algorithm is of the same order  
3 of complexity as the standard algorithm.

4 Referring now to the drawings, and more particularly to FIG.  
5 1, there is shown a presently preferred embodiment of an  
6 iterative Decision Feedback Equalizer (DFE) system 10 with hard  
7 feedback structure. In FIG. 2, there is shown the general  
8 structure of a presently preferred embodiment of an iterative DFE  
9 system 10A with soft feedback structure. Both of these iterative  
10 DFE systems 10 and 10A comprise a Decision Feedback Equalizer 12  
11 and 12A, respectively, and a decoder section 22 and 22A,  
12 respectively.

13 In FIG. 1, DFE 12 comprises feed-forward transversal filter  
14 14 to which a signal 16, such as multichannel signals with  
15 numerous inputs for receipt by matched filters, may be initially  
16 received. Thus, it will be understood that feed-forward  
17 transversal filter 14 may comprise a plurality of transversal  
18 filters or tapped delay line filters as per the prior art.  
19 Transversal filter 14 provides an equalizer structure which is  
20 followed by feedback transversal filter section 18 and symbol-by-  
21 symbol decoder 20 which acts as the de-interleaver. Feedback  
22 transversal filter 18 is preferably utilized to implement a  
23 feedback finite impulse response (FIR) filter in DFE 12. Thus,  
24 feedback transversal filter 18 is also conveniently referred to  
25 as feedback FIR filter 18 herein. An estimated symbol sequence

1 at line 21 is de-interleaved by de-interleaver 27 then applied to  
2 decoder section 22 which preferably comprises a soft-decision  
3 Viterbi decoder 24 or other suitable decoder. Output from DFE  
4 with hard feedback structure 10 is output line 26 from soft-  
5 decision Viterbi decoder 24. In high signal to noise ratios,  
6 the hard decoded symbols from soft-decision Viterbi decoder 24  
7 are more reliable than the previously detected symbols by DFE 12.  
8 In the hard-feedback embodiment of the present invention, hard  
9 values of decoded symbols of the soft decision Viterbi algorithm  
10 output from line 28 are interleaved using interleaver 29 and are  
11 iteratively used as feedback to feedback transversal filter 18,  
12 which is used to implement a feedback finite impulse response  
13 (FIR) filter in DFE 12. In a DFE with hard feedback structure  
14 10, the first iteration has the same functionality as does the  
15 prior art non-iterative structure which was discussed  
16 hereinbefore. After removing intersymbol interference (ISI) from  
17 the received signal at input 16 to produce the estimated symbol  
18 sequence at 21 by means of the de-interleaver comprised of  
19 symbol-by-symbol detector 20 and feedback transversal filter or  
20 feedback FIR filter 18, the resulting sequence can be decoded by  
21 the Viterbi decoder 24. Thus, at this first iteration, there is  
22 no difference between this system and the prior art non-iterative  
23 DFE discussed hereinbefore. However, in the subsequent  
24 iterations, DFE 12 receives the hard outputs of the decoder  
25 section 22 at feedback FIR filter 18, which may be selectively

1 effected utilizing switch 23, whereby the accuracy of output data  
2 at output 26 is improved, at least for the case of relatively  
3 high signal to noise ratios. Therefore, in one embodiment of  
4 the invention, switch 23 is effective for changing the feedback  
5 to feedback FIR filter 18 for use of the hard values of the  
6 encoded signals from the decoder section 22 after the first  
7 iteration and so long as desired.

8 Thus, system 10 is especially useful for the case of certain  
9 signal-to-noise ratios (SNRs). However, simulation results at  
10 least for a standard DFE 12 with interleaver and decoder 24  
11 operating in an iterative DFE fashion with hard feedback as per  
12 system 10 showed that for very low signal-to-noise ratios, the  
13 performance of system 10 is not satisfactory. This is because at  
14 very low SNRs, the Viterbi decoder 24 algorithm generates burst  
15 errors. Due to the subsequent error propagation of DFE 12, these  
16 errors will generate more errors in the next iterations.

17 Analyzing system 10, when we utilize the decoded values from  
18 line 28 for the coded symbols in the feedback FIR filter 12, we  
19 lose some information about the detected symbols provided by the  
20 estimated symbol sequence at line 21 from DFE 12 itself.

21 An improved approach, especially for low SNRs, is shown in  
22 the embodiment of iterative decision feedback adaptive equalizer  
23 system 10A shown in FIG. 2. In the approach of system 10A, all  
24 the information including the soft values of the coded symbols  
25 out of decoder section 22A and the soft information about the

1 detected symbols provided by the DFE 12A at line 21 in its  
 2 decision directed mode of operation. This combined information  
 3 is then used to make a symbol decision in the symbol-by-symbol  
 4 detector 20A.

5 For system 10A, the way in which we combine the two  
 6 information streams is of importance. These two information  
 7 streams are of different kinds, the soft feedback information  
 8 from the decoder 24A is of log likelihood ratio (LLR) type, but  
 9 the estimated symbol sequence  $\{\hat{I}_k\}$  at line 21 is DFE 12A estimator  
 10 output.

11 Let us assume DFE 12A is doing perfect channel equalization  
 12 at each symbol iteration and let us further assume that it can  
 13 remove all the inter-symbol interference (ISI) from the  $\{\hat{I}_k\}$   
 14 sequence. Therefore, we can calculate the LLR value for  $\{\hat{I}_k\}$  and  
 15 since we are assuming the entire ISI has been removed by the  
 16 equalizer, the estimated signal has a normal pdf with an unknown  
 17 variance. Hence:

$$18 \quad L(\hat{I}) = \ln \frac{p(c_k = +1 | \hat{I})}{p(c_k = -1 | \hat{I})} = \ln \frac{\frac{1}{\sqrt{2\pi}\sigma} \exp(-\frac{1}{2\sigma^2} |\hat{I} - 1|^2)}{\frac{1}{\sqrt{2\pi}\sigma} \exp(-\frac{1}{2\sigma^2} |\hat{I} + 1|^2)} = \frac{2}{\sigma^2} \cdot \hat{I} \quad (1)$$

19 where  $\sigma^2$  is the variance of  $\{\hat{I}_k\}$ . Now all we have to do is to  
 20 compute the variance of the estimated sequence  $\{\hat{I}_k\}$  and then  
 21 convert the estimated sequences to LLR by multiplying times the  
 22 variance log-likelihood ratio (VLLR) estimator 32 determined



1 above of  $\frac{2}{\sigma^2}$ . In the next step, we will use this LLR and other  
2 soft valued LLR of the feedback of a posteriori probabilities  
3 (APP) from the previous iterations from detector feedback line 30  
4 to make a decision in decision maker 34 of module 20A to provide  
5 hard detected signals, one possible embodiment of which is shown  
6 in greater detail in FIG. 3.

7 We can compute the variance of  $\{\hat{I}_k\}$  sequence by the following  
8 recursive equation:

$$9 \quad \sigma_k^2 = \frac{(k-1) \cdot \sigma_{k-1}^2 + (\left|\hat{I}_k\right| - 1)^2}{k} \quad (2)$$

10 In system 10B, the inputs of feedback FIR filter 18 have  
11 been replaced with the output sequence from the above described  
12 symbol-by-symbol detector 20A, an embodiment of which is shown in  
13 FIG. 3. We can see that this system will have improved  
14 performance in low SNRs compared to the standard DFE 12.

15 System 10A illustrates the general structure for iterative  
16 DFE with soft feedback. The structure of system 10A can be  
17 applied to any modulation scheme, e.g., MPSK signals. The only  
18 part of system, which needs to be modified, is decision device or  
19 symbol-by-symbol detector 20A. Unit 20A combines the information  
20 of the DFE nonlinear estimator from line 21 and the feedback LLR  
21 information from line 30 and then makes hard decision to provide  
22 hard detected signals based on the combined information for  
23 application to feedback filter 18. Depending on the type of

1 signal utilized, the structure of decision device or symbol-by-  
2 symbol detector 20A may is adjusted accordingly.

3 In regard to use of system 10A for general MPSK signals, we  
4 have seen previously that based on the assumption of correctness  
5 of all past detected symbols, minimization of the mean squared  
6 error (MSE) leads to a linear equation. The performance of a  
7 decision feed back equalizer 12 strongly depends on the quality  
8 of the previously detected symbols because any error in feedback  
9 filter 12 may cause more errors in detection of the next symbols.  
10 This is why error propagation in DFE structure may limit the  
11 performance of the system. The goal of the iterative DFE is to  
12 modify this structure so that by using the output information of  
13 the decoder from the previous iteration, we can reduce the error  
14 propagation effects. In system 10A, in the first iteration the  
15 equalizer has the same functionality as the prior art DFE. After  
16 removing the ISI from the received signal and passing through the  
17 de-interleaver the resulting sequence can be decoded by the  
18 Viterbi algorithm.

19 When we use the decoded values for coded symbols in feedback  
20 FIR 12, we lose part of the information about the detected  
21 symbols provided by the DFE itself. The best solution would be to  
22 employ all the information and then make a decision in the  
23 symbol-by-symbol detector.

24 As discussed above, the method by which we combine the two  
25 different types of information is important. The soft information

1 of the feedback is LLR, but the estimated symbol sequence  $\{\hat{y}_k\}$  is  
 2 DFE estimator outputs.

3 Similar to what was done for the BPSK case, let us assume  
 4 that the equalizer is doing perfect channel equalization in any  
 5 iteration and that it can remove all the ISI from the  
 6  $\{\hat{x}_k\}$  sequence. Therefore, we can calculate the LL value for  $\{\hat{x}_k\}$   
 7 and since we are assuming that the ISI has been removed by the  
 8 equalizer, the residual ISI plus channel noise has a normal  
 9 density with an unknown variance, and further we are assuming  
 10 that the in-phase and the quadrature noise and the residual ISI  
 11 are independent, thus:

$$12 \quad L(\tilde{I} = S(i)) = \ln p(\tilde{I}_k = S_i | \hat{x}) \quad (3)$$

$$13 \quad L(\tilde{I} = S(i)) = \ln \frac{1}{2\pi \cdot \sigma_I \sigma_Q} \exp\left(-\frac{1}{2\sigma_I^2} |\hat{x}_I - S_I(i)|^2\right) \cdot \exp\left(-\frac{1}{2\sigma_Q^2} |\hat{x}_Q - S_Q(i)|^2\right) \quad (4)$$

14 where  $\sigma_I^2, \sigma_Q^2$  are the variances of real and imaginary part of  $\{\hat{x}_k\}$ ,  
 15 respectively.  $S(i): i = 0, 1, 2, 3$ ;

$$16 \quad L(\tilde{I} = S(i)) = \ln \frac{1}{2\pi \cdot \sigma_I \sigma_Q} - \frac{1}{2\sigma_I^2} |\hat{x}_I - S_I(i)|^2 - \frac{1}{2\sigma_Q^2} |\hat{x}_Q - S_Q(i)|^2 \quad (5)$$

17 Since " $\ln \frac{1}{2\pi \cdot \sigma_I \sigma_Q}$ " is a constant it can be ignored. Hence,

$$18 \quad L(\tilde{I} = S(i)) = cte - \frac{1}{2\sigma_I^2} (\hat{x}_I^2 + S_I^2(i) - 2 \cdot \hat{x}_I \cdot S_I(i)) - \frac{1}{2\sigma_Q^2} (\hat{x}_Q^2 + S_Q^2(i) - 2 \cdot \hat{x}_Q \cdot S_Q(i)) \quad (6)$$

19 and

$$L(\tilde{I} = S(i)) = cte + \frac{1}{\sigma_I^2} \cdot \hat{x}_I \cdot S_I(i) + \frac{1}{\sigma_Q^2} \cdot \hat{x}_Q \cdot S_Q(i) \quad (7)$$

This last equation represents a general technique to calculate the log likelihood value for non-linear estimations in DFE systems for all I-Q modulation types. For this particular case with QPSK modulation, we have:

$$L(\tilde{I} = S(i))|_{i=0,1,2,3} = \pm \frac{\sqrt{2}}{2\sigma_I^2} \cdot \hat{x}_I \pm \frac{\sqrt{2}}{2\sigma_Q^2} \cdot \hat{x}_Q \quad (8)$$

Now all we need to do is to compute the variances of the estimated sequence  $\{\hat{x}_k\}$  and then convert these estimated sequences to LL. The variances values for the in-phase and the quad-phase parts can be calculated by recursive equations:

$$\sigma_{I_k}^2 = \frac{(k-1) \cdot \sigma_{I_{k-1}}^2 + \left( \left| \hat{x}_{I_k} \right| - \frac{1}{\sqrt{2}} \right)^2}{k} \quad (9)$$

$$\sigma_{Q_k}^2 = \frac{(k-1) \cdot \sigma_{Q_{k-1}}^2 + \left( \left| \hat{x}_{Q_k} \right| - \frac{1}{\sqrt{2}} \right)^2}{k} \quad (10)$$

Accordingly, FIG. 4 shows the new structure for the symbol-by-symbol detector unit 20A in an iterative soft DFE system for QPSK modulation. Again estimated sequence from 21  $\{\hat{x}_k\}$  is applied as indicated having real and imaginary parts as shown divided in block 36. Variance estimators 38 and 40 are implemented as per the equations directly above. The signal is then multiplied by the likelihood ratio (LLR) estimator 32A  $\frac{\sqrt{2}}{2\sigma_Q^2}$  and 32B  $\frac{\sqrt{2}}{2\sigma_I^2}$  as per

1 the equations illustrated above. Real and imaginary parts  
2 generated by LLR estimators 32A and 32B are reintegrated in block  
3 42.

4 In summary, the embodiments shown by the present invention  
5 replace the standard DFE structure with an iterative structure  
6 that combines the DFE and the decoder block. The hard-iterative  
7 DFE system 10 iterates the normal DFE 12 followed by a de-  
8 interleaver 27 and decoder 22 which preferably utilizes soft  
9 Viterbi decoder 24. In this fashion, the most likely coded or  
10 hard encoded symbols of decoder 22 are interleaved at interleaver  
11 29 and passed back to DFE 12 as the new training sequence to be  
12 used as the new reference instead of using the decision directed  
13 mode of prior art equalizer operation as in the first pass.

14 The soft-iterative DFE system 10A replaces one preferred  
15 embodiment of soft Viterbi decoder 24 with a Maximum A posteriori  
16 Probability (MAP) decoder 24A which serves to make better use of  
17 the advantages of channel coding to improve the channel  
18 equalization-detection process. Embodiment 10A incorporates new  
19 information to help make more reliable symbol decisions. MAP  
20 decoder 24A is connected to the DFE 12A through an interleaver  
21 for the decoded symbols and a de-interleaver for the encoded  
22 symbols. After the initial pass through the system, iterations  
23 of the soft-iterative DFE system (multiple passes through the  
24 system or loops through the system), the decoded reference  
25 signal's LLR values from decoder 24A are combined with the

1 decision directed equalizer symbol estimates from line 21 by  
2 using variance log-likelihood ratio estimator 32. These combined  
3 LLR values are then passed to symbol by symbol detector 20A that  
4 determines which symbol of the possible symbols was detected and  
5 then feeds back this symbol estimate to feedback filter 18 so  
6 that the next sequential symbol can be processed. This  
7 iterative processing continues either for a fixed number of  
8 iterations has occurred or when a stop criterion based has been  
9 passed.

10 The performance improvement in the hard-iterative scheme is  
11 due to using corrected symbols to feedback during subsequent  
12 iterations and the performance improvement in the soft-iterative  
13 technique is due to using a MAP decoder instead of a Viterbi  
14 decoder, iterating the combined equalizer and decoder sections a  
15 number of times, combining the decision directed LLR symbol  
16 estimates with the decoder's LLR estimates to better determine  
17 the symbol to feedback within the equalizer for each symbol in  
18 the data packet.

19 It will be understood that features of the present invention  
20 may also be utilized in other types of communication systems than  
21 underwater communication systems. Many additional changes in the  
22 details, components, steps, algorithms, and organization of the  
23 system, herein described and illustrated to explain the nature of  
24 the invention, may be made by those skilled in the art within the  
25 principle and scope of the invention. It is therefore understood

- 1 that within the scope of the appended claims, the invention may
- 2 be practiced otherwise than as specifically described.